

Research Article

Structural Analysis for a Composite Parallel Beam Structures Using QSE 7 Staad Pro Software in Accordance to BS 5950- 1 Advanced UK Beams

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Abstract: This technical paper presents a structural analyzing and manual calculations for a composite Parallel Beam with Steel class (S275) and Concrete class (C30/37) with a Decking (Ribdeck AL) a single unpropped support condition, 1mm gauge, 0.103 kN/m² Self weight, assumed slab depth 150mm from RLSD website with a concrete volume is 0.125 m³/m². The calculations includes bending design, shear stress, shear connection, deflection (Elastic), checking of non-composite state, bending design and shear stress of spine beam. Furthermore, the forces, shear and bending moment diagrams for rib beam are also presented (using QSE 7 Staad Pro). As per BS 5950- 1 Advanced UK Beams.

Keywords: Composite parallel beam, structural analysis, BS 5950-1 Advanced UK beams, QSE 7 Staad Pro.

1.INTRODUCTION

The dimensions of the parallel beam are L1 = 5.1 m, L2 = 8.1 m

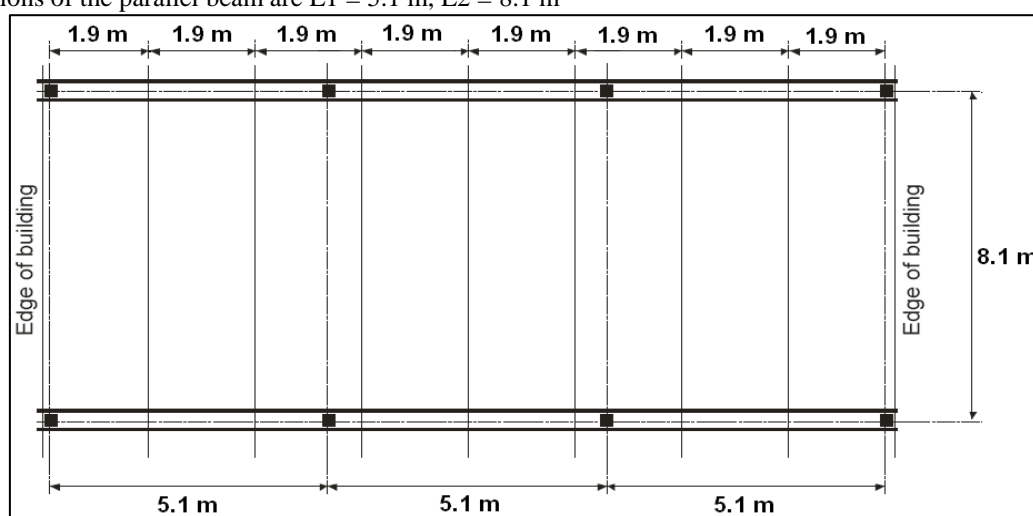


Figure 1: Top view of the analyzed parallel beam.

1.1 Material used

- Steel (S275) $f_{yk} = f_{yd} = 275 \text{ N/mm}^2$

- Concrete (C30/37) $f_{ck} = 30 \text{ N/mm}^2$

- Decking (Ribdeck AL) support condition: Single – unpropped

Gauge = 1.0 mm

Self weight = 0.103 kN/m²

Assumed slab depth 150mm from RLSD website the concrete volume is 0.125 m³/m²

Quick Response Code



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1.2 Loading

- Self weight of concrete	$24 \text{ kN/m}^3 \times 0.125 \text{ m}^3/\text{m}^2 = 3.000 \text{ kN/m}^2$
- Self weight of decking	$= 0.103 \text{ kN/m}^2$
- Dead load	$= 1.200 \text{ kN/m}^2$
Total Dead load	$= 4.303 \text{ kN/m}^2$

Live Load	$= 3.000 \text{ kN/m}^2$
Total Load	$(1.35 \times 4.303 \text{ kN/m}^2) + (1.5 \times 3.000 \text{ kN/m}^2) = 10.31 \text{ kN/m}^2$

2.METHODOLOGY

2.1 Rib beam

- Loading on rib beam $= 10.31 \text{ kN/m}^2 \times 1.9 \text{ m}$
 $= 19.59 \text{ kN/m}$
- Loading on spine beam $= 19.59 \text{ kN/m} \times 8.1 \text{ m} \times 0.5$
 $= 79.34 \text{ kN}$
- M_{Max} $= w \times l^2 / 8$ (1)
 $= 19.59 \times 8.1^2 / 8$
 $= 161 \text{ kNm}$
- M_x $= 3 \times w \times l^2 / 32$ (2)
 $= 3 \times 19.59 \text{ kN/m} \times (8.1 \text{ m})^2 / 32$
 $= 120.5 \text{ kNm}$

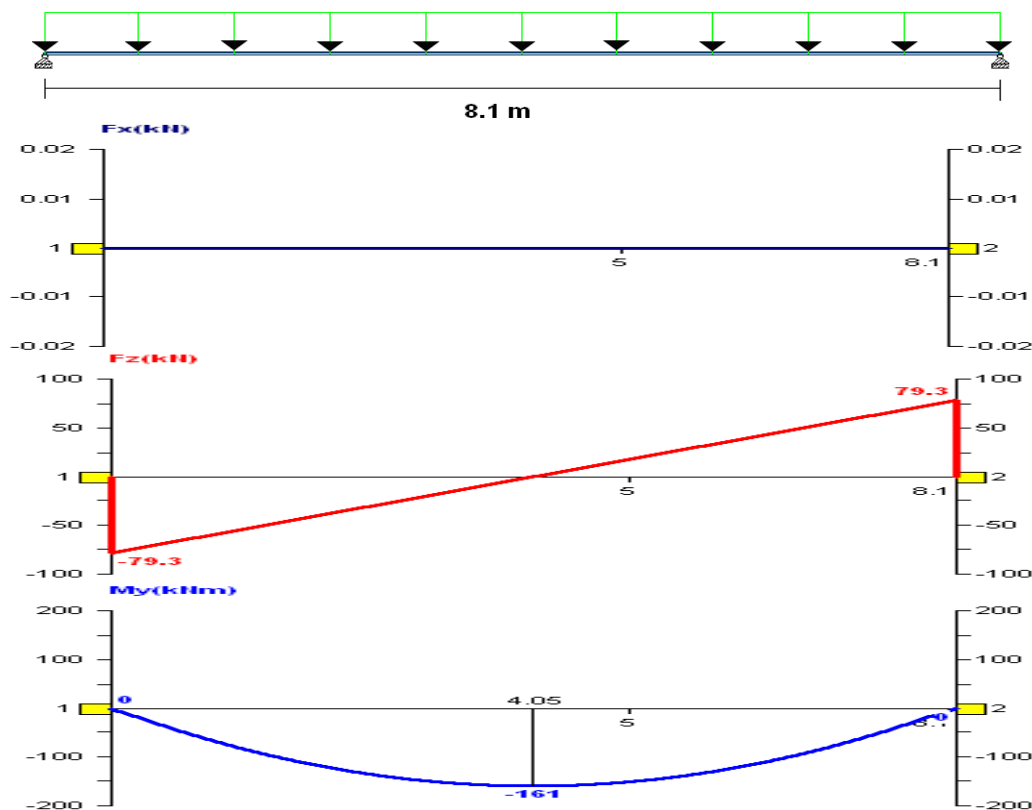


Figure 2: Forces, shear and bending moment diagrams for rib beam (using QSE 7 Staad Pro).

2.2 Bending Design

- $b_{eff} = 0.25 \times L$ (3)
 $= 0.25 \times 8.1 \text{ m} = 2.03 \text{ m}$
- Assuming steel beam carries 50% so,
- $M_{Ed} = 80.5 \text{ kNm}$

Note: we are using S275, therefore, the value of f_{yd} will be 275 kN/mm^2

- $S_x = M_{Ed} / f_{yd}$ (4)
 $= (80.5 \text{ kNm} \times 10^6) / (275 \text{ kN/mm}^2 \times 10^3) = 293 \text{ cm}^3$

- From BS 5950- 1 (Advanced UK Beams),

use section 254 x 146 x 37

$$S_x = 483 \text{ cm}^3, A = 47.2 \text{ cm}^2$$

$$\begin{aligned} - T_d &= A \times f_{yd} & (5) \\ &= (47.2 \text{ cm}^2 \times 10^2 \times 275 \text{ N/mm}^2) / (10^3) \\ &= 1298 \text{ kN} \end{aligned}$$

$$\begin{aligned} - T_d &= C_d \\ &= 0.85 \times \alpha_c \times (f_{ck} / \delta_c) \times b_{eff} \times z & (6) \end{aligned}$$

Thus,

$$\begin{aligned} - Z &= (T_d \times \delta_c) / (0.85 \times \alpha_c \times f_{ck} \times b_{eff}) & (7) \\ &= [(1298 \text{ kN} \times 1.5) / (0.85 \times 0.85 \times 30 \text{ N/mm}^2 \times 2030\text{mm})] \times 10^3 \\ &= 44 \text{ mm} \end{aligned}$$

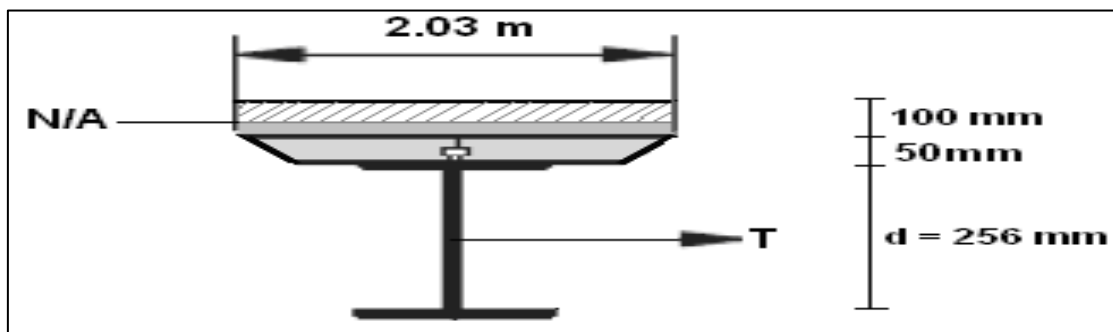


Figure 3: Section view of the beam.

$$\begin{aligned} d &= 256 \text{ mm} \\ \text{Thickness} &= 150 \text{ mm} \\ \text{Overall depth} &= 406 \text{ mm} \\ \frac{1}{2} Z &= 22 \text{ mm} \\ &= 384 \text{ mm} \\ b_{eff} &= 203 \text{ mm} \\ x &= 181 \text{ mm} \end{aligned}$$

$$\begin{aligned} - M_{pl,Rd} &= T_d \times \text{lever arm} & (8) \\ &= C_d \times x \\ &= (1298 \text{ kN} \times 0.181 \text{ m}) \\ &= 235 \text{ kNm} > 161 \text{ kNm} & \text{OK} \end{aligned}$$

$$\begin{aligned} - M_{pl,a,Rd} &= f_{yd} \times S_x & (9) \\ &= (275 \text{ N/mm}^2 \times 483 \text{ cm}^3) / 10^3 \\ &= 132.8 \text{ kNm} > 80.5 \text{ kNm} & \text{OK} \end{aligned}$$

2.3 Shear stress

$$\begin{aligned} \text{Section } 254 \times 146 \times 37 & \quad A = 47.2 \text{ cm}^2 & \quad t = 6.3 \text{ mm} \\ & \quad B = 146.4 \text{ mm} & \quad r = 7.6 \text{ mm} \\ & \quad T = 10.9 \text{ mm} \end{aligned}$$

$$\begin{aligned} - A_{shear} &= A - 2 \times T \times (B - t - 2r) & (10) \\ &= 4720 \text{ mm}^2 - 2 \times 10.9 \text{ mm} \times (146.4 \text{ mm} - 6.3 \text{ mm} - 2 \times 7.6 \text{ mm}) \\ &= 1997 \text{ mm}^2 = 20 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} - V_{pl,a,Rd} &= A_{shear} \times (f_{yd} / \sqrt{3}) & (11) \\ &= 20 \text{ cm}^2 \times (27.5 \text{ kN/cm}^2 / \sqrt{3}) \\ &= 317.5 \text{ kN} > 79.34 \text{ kN} & \text{OK} \end{aligned}$$

3.RESULTS

3.1 Shear connection

The below equations has been used and the lower value of them was considered for the number of shear connection.

$$1. P_{Rd} \text{ Steel} = (0.8 \times f_u \times \pi \times d^2) / (4 \times \delta_v) \quad (12)$$

$$2. P_{Rd} \text{ Concrete} = [0.29 \times \alpha \times d^2 \times \sqrt{(f_{ck} \times E_{cm})}] / \delta_v \quad (13)$$

$$\begin{aligned} \text{Assumed } f_u &= 450 \text{ N/mm}^2 & \alpha &= 1 \\ \text{Stud diameter } d &= 20 \text{ mm} & f_{ck} &= 30 \text{ N/mm}^2 \\ \delta_v &= 1.25 & E_{cm} &= 33000 \text{ N/mm}^2 \\ \text{Assumed } h_{SC} / d &> 4 \end{aligned}$$

$$\begin{aligned} - P_{Rd} \text{ Steel} &= [(0.8 \times f_u \times \pi \times d^2) / (4 \times \delta_v)] / 10^3 \\ &= (0.8 \times 450 \text{ N/mm}^2 \times \pi \times 20^2) / (4 \times 1.25) \\ &= 90.48 \text{ kN} \end{aligned}$$

$$\begin{aligned} - P_{Rd} \text{ Concrete} &= (0.29 \times \alpha \times d^2 \times \sqrt{f_{ck} \times E_{cm}}) / \delta_v \\ &= [0.29 \times 1 \times 20^2 \times \sqrt{(30 \text{ N/mm}^2 \times 33000 \text{ N/mm}^2)}] / 1.25 \\ &= 73.7 \text{ kN} \end{aligned}$$

Note: $P_{Rd} \text{ Concrete } 73.7 \text{ kN} < P_{Rd} \text{ Steel } 90.48 \text{ kN}$, therefore, choose $P_{Rd} \text{ Steel}$ since it is lower than Concrete.

$$- N = F / F_{Stud} \quad \text{where } F = M_x / l_a \quad (14)$$

$$F = 120.5 \text{ kNm} / 0.181 \text{ m} = 665.7 \text{ kN}$$

$$\text{and } F_{Stud} = P_{Rd} \text{ Concrete} = 73.7 \text{ kN} \quad (15)$$

$$\begin{aligned} \text{Thus, } N &= F / F_{Stud} \\ N &= 665.7 \text{ kN} / 73.7 \text{ kN} = 9.03 \approx 10 \end{aligned}$$

Number of shear connectors over first/last 2.03m, $N \approx 10$ shear connectors over 2.03 m @ 200mm spacing $\geq 5d$

$$- N = F / F_{Stud} \quad \text{where } F = (M_{Max} - M_x) / l_a \quad (16)$$

$$F = (161 \text{ kNm} - 120.5 \text{ kNm}) / 0.181 \text{ m} = 223.8 \text{ kN}$$

$$\text{and } F_{Stud} = P_{Rd} \text{ Concrete} = 73.7 \text{ kN}$$

$$\begin{aligned} \text{Thus, } N &= F / F_{Stud} \\ N &= 223.8 \text{ kN} / 73.7 \text{ kN} = 3.04 \approx 4 \end{aligned}$$

Number of shear connectors over middle 2.02m, $N \approx 4$ shear connectors over 2.02 m @ 510mm spacing $\geq 5d$

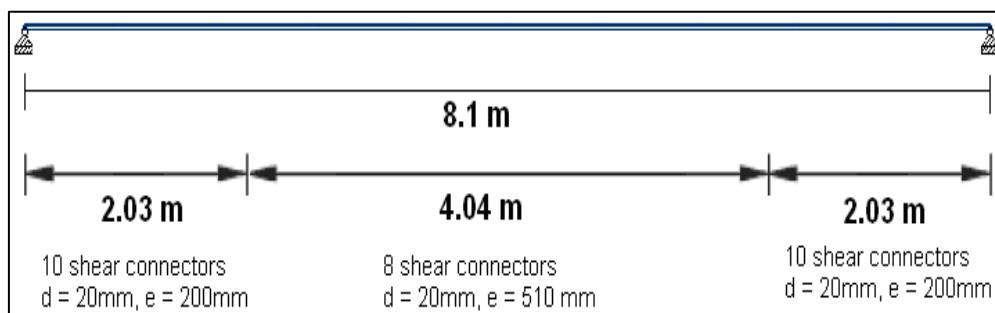


Figure 4: Distribution of shear connectors with dimensions through the beam.

3.2 Deflection (Elastic)

$$\begin{aligned} - \text{Loading on rib beam} &= (4.303 \text{ kN/m}^2 + 3.0 \text{ kN/m}^2) \times 1.9 \text{ m} \\ &= 13.9 \text{ kN/m} \end{aligned}$$

$$\begin{aligned} - m &= E_s / E_{cm} \\ &= 205000 \text{ N/mm}^2 / 33000 \text{ N/mm}^2 = 6.21 \end{aligned} \quad (17)$$

$$\begin{aligned} - \text{Section } 254 \times 146 \times 37 &\sim \text{Area of section} = 47.2 \text{ cm}^2 \\ - \text{Width} &= b_{eff} \times E_{cm} / E_s \\ &= (2.03 \text{ m} \times 33000 \text{ N/mm}^2) / 205000 \text{ N/mm}^2 \\ &= 0.327 \text{ m} \end{aligned} \quad (18)$$

$$\begin{aligned} - A_c &= b \times h \\ &= 327 \text{ mm} \times 150 \text{ mm} = 49050 \text{ mm}^2 \end{aligned} \quad (19)$$

$$- L_a = 0.5 \times h_C + H = 0.5 \times 150\text{mm} + 256 \text{ mm} = 331 \text{ mm} \tag{20}$$

$$- M_C = A_C \times L_a = 49050 \text{ mm}^2 \times 331 \text{ mm} = 16235550 \text{ mm}^3 \tag{21}$$

$$- A_S = 4720 \text{ mm}^2$$

$$- L_a = 0.5 \times H = 0.5 \times 256 \text{ mm} = 128 \text{ mm}$$

$$- M_S = A_S \times l_a = 4720 \text{ mm}^2 \times 128 \text{ mm} = 604160 \text{ mm}^3 \tag{22}$$

$$- \text{Neutral Axis} = (M_C + M_S) / (A_C + A_S) = (16235550 \text{ mm}^3 + 604160 \text{ mm}^3) / (49050 \text{ mm}^2 + 4720 \text{ mm}^2) = 313.2 \text{ mm} \tag{23}$$

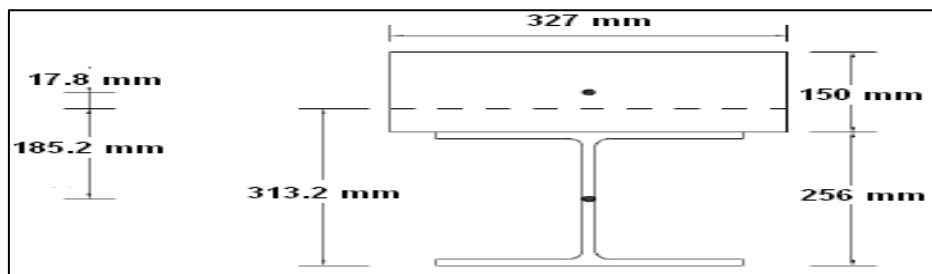


Figure 5: Geometry of the beam section.

Table 1: Moment of Inertia of the analyzed parallel beam.

Description	A (mm ²)	r (mm)	Ar ² (mm ⁴)	Iyy (mm ⁴)
Concrete	49050	17.8	15021563	91968750
Beam	4720	185.2	161891469	55370000
Σ			176913032	147338750

The inertia of the section is the sum of Ar² and Iyy.

$$\text{Thus, } I = \sum Ar^2 + \sum Iyy = 176913032 + 147338750 = 324251782 \text{ mm}^4 \tag{24}$$

$$- \delta_{\text{Max}} = L / 300 = 8.1 \text{ m} / 300 = 27 \text{ mm} \tag{25}$$

$$\delta = \frac{5wL^4}{384EI} = \frac{5 \times 19.59 \text{ N} / \text{mm} \times (8100\text{mm})^4}{384 \times 205000 \text{ N} / \text{mm}^2 \times 324251782 \text{ mm}^4} \tag{26}$$

$$= 16.5 \text{ mm} \leq \text{span} / 300 = 27 \text{ mm} \quad \text{OK}$$

3.3 Checking of non-composite state

Loading:

$$- \text{Self weight of concrete} = 24 \text{ kN/m}^3 \times 0.125 \text{ m}^3/\text{m}^2 = 3.000 \text{ kN/m}^2$$

$$- \text{Self weight of decking} = 0.103 \text{ kN/m}^2$$

$$\text{Total Dead load} = 3.103 \text{ kN/m}^2$$

$$\text{Live Load} = 1.500 \text{ kN/m}^2$$

$$\text{Total Load} = (1.35 \times 3.103 \text{ kN/m}^2) + (1.5 \times 1.500 \text{ kN/m}^2) = 6.439 \text{ kN/m}^2$$

$$- \text{Loading on rib beam} = 6.439 \text{ kN/m}^2 \times 2.03 \text{ m} = 13.07 \text{ kN/m}$$

$$- M_{Ed} = 13.07 \text{ kN/m} \times (8.1 \text{ m})^2 / 8 = 107.20 \text{ kNm}$$

$$- M_{el,a,Rd} = f_{yd} \times S_x = (275 \text{ N/mm}^2 \times 433 \text{ cm}^3) / 10^3 = 119.08 \text{ kNm} > 107.20 \text{ kNm} \quad \text{OK}$$

3.4 Spine beam

$$-p = w \times l / 2 = 19.59 \text{ kN/m} \times 8.1 \text{ m} / 2 = 79.34 \text{ kN}$$

The reaction R1, R2, R3 and R4 has been obtained from QSE 7 Staad Pro and the values were as follows:

$$\begin{aligned} R1 &= 147.56 \text{ kN} \\ R2 &= 209.47 \text{ kN} \\ R3 &= 209.47 \text{ kN} \\ R4 &= 147.56 \text{ kN} \end{aligned}$$

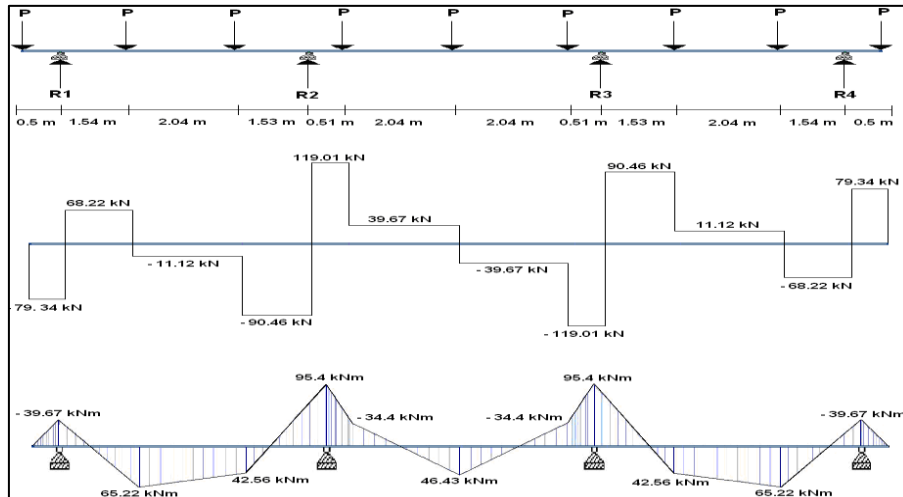


Figure 6: The below illustrates the forces, shear and bending moment diagrams for spine beam (using QSE 7 Staad Pro).

4.CONCLUSION

4.1 Bending design

$$\begin{aligned} \text{Max } M_{Ed} &= 95.4 \text{ kNm} \\ -S_x &= M_{Ed} / f_{yd} \\ &= (95.4 \text{ kNm} / 275 \text{ N/mm}^2) \times 10^3 = 347 \text{ cm}^3 \end{aligned}$$

- From BS 5950- 1 (Advance UK Beams), use section 305 x 102 x 33
 $S_x = 481 \text{ cm}^3$, $A = 41.8 \text{ cm}^2$

$$\begin{aligned} -M_{pl,a,Rd} &= f_{yd} \times S_x \\ &= (275 \text{ N/mm}^2 \times 481 \text{ cm}^3) / 10^3 \\ &= 132.3 \text{ kNm} > 95.4 \text{ kNm} \quad \text{OK} \end{aligned}$$

4.2 Shear Stress

$$\begin{aligned} \text{- Section } 305 \times 102 \times 28 \quad A &= 41.8 \text{ cm}^2 & t &= 6.6 \text{ mm} \\ B &= 102.4 \text{ mm} & r &= 7.6 \text{ mm} \\ T &= 10.8 \text{ mm} \end{aligned}$$

$$\begin{aligned} -A_{\text{shear}} &= A - 2 \times T \times (B - t - 2r) \\ &= 4180 \text{ mm}^2 - 2 \times 10.8 \text{ mm} \times (102.4 \text{ mm} - 6.6 \text{ mm} - 2 \times 7.6 \text{ mm}) \\ &= 2439 \text{ mm}^2 = 24.4 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} -V_{pl,a,Rd} &= A_{\text{shear}} \times (f_{yd} / \sqrt{3}) \\ &= 24.4 \text{ cm}^2 \times (27.5 \text{ kN/cm}^2 / \sqrt{3}) \\ &= 387.4 \text{ kN} > 119.01 \text{ kNm} \quad \text{OK} \end{aligned}$$

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